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Fig. 9. Possible alternative  $CaCO_3$  stability diagrams. Figure 9A shows possible relations if a hypothetical phase "X" makes a metastable triple point with aragonite and calcite II in the field of aragonite. Metastable portions are indicated by dotted and broken lines. Figure 9B shows possible relations if a hypothetical phase "X" has a stable invariant relation with respect to calcite I and calcite II.

does, and the  $\Delta_{I-II}$  must be the sum of  $\Delta V_{I-X}$  and  $\Delta V_{X-II}$ . This hypothesis would also eliminate the need for curvature in the calcite I-II curve. A deflection of the calcite-aragonite curve by the II-X transition as it crosses it might be too small to be easily observed.

Figure 9B is a diagram that would result if there is a "II-X" transition that makes a stable invariant point with the I-II transition. The observations of Bell and England could be explained by this hypothesis, but the observation of Dandekar could not. Again the I-II transition would have to have a large  $\Delta V$  and need not have much curvature.

It is conceivable that both calcite II and a "calcite X" might have a calcite I-like X-ray diffraction powder pattern with the (113) line missing, whether or not an anion-rotation phenomenon is responsible for the line deletion. Thus a diagram involving three calcite phases is not eliminated as a possibility by the present data. The scientists' prejudice for the simplest workable hypothesis may lend favor to the relatively straightforward calcite I-II interpretation as shown in figure 1.

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Binary system.—Many of the features of the pressure-temperature diagram of the system  $CaCO_3$ -MgCO<sub>3</sub> can be investigated by using the theory of regular solutions. Following Robie (1957), CaCO<sub>3</sub> (cc)-MgCO<sub>3</sub> (mc) solutions in the calcite structure are treated as regular solutions, so that:

$$\mu_{\rm ec} = \mu^{\circ}_{\rm cc} + \operatorname{RT} \ln (1 \cdot X_{\rm mc}) + \Omega X^{2}_{\rm mc}$$
$$\mu_{\rm mc} = \mu^{\circ}_{\rm mc} + \operatorname{RT} \ln X_{\rm mc} + \Omega (1 \cdot X_{\rm mc})^{2}$$

where  $\mu$  denotes the partial molal Gibbs energy of the components, R is the gas constant per mole, T is the absolute temperature, X is the mole fraction of a component,  $\Omega$  is the "inter-change energy" per mole (Guggenheim, 1952), and a superscript zero refers to the pure component.

The equilibrium relation of the solvus is given by:

$$\mu_{\rm cc}{}^{\rm c} + \mu_{\rm mc}{}^{\rm c} - \mu^{\rm p} = 0$$

Here the superscript C represents calcite, and D represents dolomite. Inserting the regular solution equations gives:

$$0 = \Delta \mu^{\circ} + RT \ln X_{mc} (1-X_{mc}) + \Omega [X_{mc}^{2} + (1-X_{mc})^{2}]$$

The standard Gibbs energy change for the pure substances,  $\Delta \mu^{\circ}$ , is evaluated by:

$$\Delta \mu^{\circ} \equiv \Delta \mathrm{H}^{\circ}_{298} - \mathrm{T} \Delta \mathrm{S}^{\circ}_{298}$$

where  $\Delta H^{\circ}_{298}$  is the standard enthalpy change, and  $\Delta S^{\circ}_{298}$  is the corresponding entropy increment. The latter equation assumes that  $\Delta S^{\circ}$  is constant over the temperature interval 298°K-T, an assumption that is necessary because of the lack of high-temperature heat content data for magnesite and dolomite. This assumption is likely to be valid with a high degree of accuracy in the temperature range of interest, as evidenced by the fact that the heat capacity of dolomite in the range 70 to 300°K is equal to the sum of the heat capacities of calcite and magnesite to within 0.2 percent (Robie, ms, p. 73). Hence,

$$\Omega = \frac{-\Delta H^{\circ}_{298} + T \Delta S^{\circ}_{298} - RT \ln X_{mc}(1-X_{mc})}{2X^{2}_{mc} - 2X_{mc} + 1}$$

The values of  $\Delta H^{\circ}_{298} = 3150$  cal/mole and  $\Delta S^{\circ}_{298} = 0.81$  cal/°C-mole used by Robie are adopted. Table 4 shows the values of  $\Omega$  that are calculated at several temperatures when the best solvus data of the present work, reduced to a 1-atm basis by applying the measured pressure correction, are used. The  $\Omega$  values fall within a fairly narrow spread, which is some justification for the use of the regular solution theory.

The effect of total pressure on the MgCO<sub>3</sub> solubility can be calculated as follows. The total variation at constant temperature of the Gibbs energy change of the solvus reaction,  $\Delta \mu = \mu_{cc}^{\ c} + \mu_{mc}^{\ c} - \mu^{\ p}$ ,